INTEREST RATE UNCERTAINTY AS A POLICY TOOL

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July 24, 2019 CBC-IMF-*IMF Economic Review* Conference Santiago, Chile

INTRODUCTION

Figure: Portfolio Flows to Emerging Markets (13-week moving average, bn USD)



INTEREST RATE CORRIDOR

Figure: Interest rate corridor and average funding cost, Turkey



PORTFOLIO AND FDI FLOWS

Figure: Financing the current account, Turkey (12-month cumulative, bn USD)



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- Does an increase in the volatility of domestic interest rate affect the composition of capital inflows between bonds and FDI?
- What are the possible trade-offs that are faced by a central banker in navigating among price stability and controlling the external account?

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 - Endogenous movements in markups driven by nominal price and wage rigidities

WHAT WE DO (1)

- Developing an open macroeconomic model in which the central bank uses the interest rate volatility as a policy tool
 - Distinguish between bond and FDI flows
 - Incomplete international financial markets: NFA important for transmission of volatility shocks
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A New Keynesian Open Economy framework that enables us to decompose the current account into bond and FDI components easily (Bergin (2006), Obstfeld and Rogoff (1995))

• Stochastic volatility process (Justiniano and Primiceri (2008))

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- Model solution using a third-order perturbation (Fernandez-Villaverde et alii (2015))
- IRF calculation from the stochastic steady-state (Born and Pfeifer (2014a) and (2014b))
 - Ergodic distribution of the endogenous variables move away from their deterministic steady state
 - SSS: Ergodic Mean in the Absence of Shocks (EMAS)

[►] Illustration of stochastic steady state

NEW INSIGHTS (1)

- Using interest rate uncertainty as a policy tool has different implications on bond and FDI component of the current account
 - Portfolio risk and precautionary savings channels (Bond component)
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 - Markup channel (FDI component)
 - ★ The ability to create a negative comovement is dependent on the type of price stickiness
- Using uncertainty as a policy tool might be useful in adjusting the current account, but at the expense of lower output and higher inflation

NEW INSIGHTS (2)

- If FDI irreversible, fluctuations in the FDI-component of the CA are milder
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- ELB in the rest of the world:
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- Risk aversion of foreign agents is important:
 - Amplified reaction of the current account
 - Deviations in UIP imply short-term inflows

THE MODEL ARCHITECTURE

Emerging Market Economy



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Emerging Market Economy



• Expected intertemporal utility:

$$\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \left[\frac{C_t(h)^{1-\rho}}{1-\rho} - \chi \frac{L_t(h)^{1+\varphi}}{1+\varphi} \right]$$

• Budget constraint:

 $P_tC_t(h) + B_{t+1}(h) + S_tB_{*,t+1}(h) + adj_t + P_tI_t(h) + S_tP_t^*I_{*,t}(h)$

 $= R_t B_t(h) + S_t R_t^* B_{*,t}(h) + W_t(h) L_t(h) + P_t r_{K,t} K_t(h) + S_t P_t^* r_{K,*,t} K_{*,t}(h)$

$$-\frac{\kappa^{W}}{2} \left(\frac{W_{t}(h)}{W_{t-1}(h)} - 1\right)^{2} W_{t}(h) L_{t}(h) + \Pi_{t} + T_{t}^{f*}$$

Other constraints:

$$L_t(h) = \left(\frac{W_t(h)}{W_t}\right)^{-\epsilon_W} L_t$$

$$K_{t+1}(h) = (1-\delta)K_t(h) + I_t(h)$$

$$K_{*,t+1}(h) = (1-\delta)K_{*,t}(h) + I_{*,t}(h)$$

FOCs:

$$w_t = \mu_t^W \left(\frac{\chi L_t^{\varphi}}{C_t^{-\rho}} \right)$$

$$1 = q_t$$

$$1 = \beta \mathbb{E}_t \left[\left(\frac{C_{t+1}}{C_t} \right)^{-\rho} \left(r_{K,t+1} + (1-\delta) \right) \right]$$

Investment to the RoW:

 $rer_t = q_{*,t}$

$$1 = \beta \mathbb{E}_t \left[\left(\frac{C_{t+1}}{C_t} \right)^{-\rho} \frac{rer_{t+1}}{rer_t} \left(r_{K,*,t+1} + 1 - \delta \right) \right]$$

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Similarly, price of FDI coming into the EME:

$$\frac{1}{rer_t} = q_t^*$$

$$1 = \beta \mathbb{E}_t \left[\left(\frac{C_{t+1}^*}{C_t^*} \right)^{-\rho} \frac{\operatorname{rer}_t}{\operatorname{rer}_{t+1}} \left(r_{K,t+1}^* + 1 - \delta \right) \right]$$

Firms

Intermediate Goods producers:

$$Y_{H.t}(i) + \left(\frac{1-n}{n}\right)Y_{H,t}^{*}(i) = (K_t(i))^{\alpha_1} (K_t^{*}(i))^{\alpha_2} L_t(i)^{1-\alpha_1-\alpha_2}$$

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Final Goods producers:

$$Y_t = \left(a^{\frac{1}{\omega}}Y_{H,t}^{\frac{\omega-1}{\omega}} + (1-a)^{\frac{1}{\omega}}Y_{F,t}^{\frac{\omega-1}{\omega}}\right)^{\frac{\omega}{\omega-1}}$$

Firms' problem

► Resource Constraints

NET FOREIGN ASSET ACCUMULATION

$$b_{t+1} + rer_t b_{*,t+1} + \left(\frac{1-n}{n}\right) rer_t K_{*,t+1} - K_{t+1}^*$$

$$= \frac{R_{t}}{\Pi_{t}}b_{t} + \frac{R_{t}^{*}}{\Pi_{t}^{*}}rer_{t}b_{*,t} + \left(\frac{1-n}{n}\right)rer_{t}(r_{K,*,t}+1-\delta)K_{*,t} - \left(r_{K,t}^{*}+1-\delta\right)K_{t}^{*} + \underbrace{\left(\frac{1-n}{n}\right)\mu_{H,t}^{*}mc_{t}Y_{H,t}^{*} - rer_{t}\mu_{F,t}mc_{t}^{*}Y_{F,t}}_{n}$$

Trade Balance

DECOMPOSING THE CURRENT ACCOUNT

$$\underbrace{(b_{t+1} - b_t) + rer_t (b_{*,t+1} - b_{*,t})}_{(b_{t+1} - b_t) + rer_t (b_{*,t+1} - b_{*,t})}$$

Bond component

$$+\underbrace{\left(\frac{1-n}{n}\right)rer_t\left(K_{*,t+1}-K_{*,t}\right)-\left(K_{t+1}^*-K_t^*\right)}_{\text{FDI component}} \equiv CA_t$$

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MONETARY AUTHORITY

• Fisher relation:

$$R_{t+1} = (1 + r_{t+1}) \mathbb{E}_t \Pi_{t+1}$$

• Domestic interest rate rule:

$$\frac{R_t}{R} = \left(\frac{R_{t-1}}{R}\right)^{\rho_R} \left(\frac{\Pi_t}{\Pi}\right)^{(1-\rho_R)\rho_\Pi} \left(\frac{Y_t}{Y}\right)^{(1-\rho_R)\rho_Y} e^{u_t}$$

with

$$u_t = \rho^u u_{t-1} + e^{\sigma_t^R} \varepsilon_t$$

and

$$\sigma_t^R = (1 - \rho^{\sigma^R})\sigma^R + \rho^{\sigma^R}\sigma_{t-1}^R + \varepsilon_t^{\sigma}$$

PORTFOLIO RISK

• Relative risk premia between the RoW investor's assets:

$$RR_{B_{*}^{*},B^{*},t+1} \equiv \frac{Cov_{t}\left(\beta_{t,t+1}^{*},\frac{R_{t+1}^{*}}{\Pi_{t+1}^{*}} - \frac{rer_{t}}{rer_{t+1}}\frac{R_{t+1}}{\Pi_{t+1}}\right)}{\mathbb{E}_{t}\left[\beta_{t,t+1}^{*}\right]}$$

$$RR_{K_{*}^{*},K^{*},t+1} \equiv \frac{Cov_{t}\left(\beta_{t,t+1}^{*},R_{K_{*}^{*},t+1} - \frac{rer_{t}}{rer_{t+1}}R_{K^{*},t+1}\right)}{\mathbb{E}_{t}\left[\beta_{t,t+1}^{*}\right]}$$

$$RR_{B^{*},K^{*},t+1} \equiv \frac{Cov_{t}\left(\beta_{t,t+1}^{*},\frac{rer_{t}}{rer_{t+1}}\left(\frac{R_{t+1}}{\Pi_{t+1}} - R_{K^{*},t+1}\right)\right)}{\mathbb{E}_{t}\left[\beta_{t,t+1}^{*}\right]}$$

where $R_K \equiv 1 - \delta + r_K$.

OUR EXPERIMENT



Calibration

Model Solution




$$RR_{B_*^*,B^*,t+1} \equiv \frac{Cov_t \left(\beta_{t,t+1}^*, \frac{R_{t+1}^*}{\Pi_{t+1}^*} - \frac{rer_t}{rer_{t+1}} \frac{R_{t+1}}{\Pi_{t+1}}\right)}{\mathbb{E}_t [\beta_{t,t+1}^*]}$$





$$RR_{\mathcal{K}^*_*,\mathcal{K}^*,t+1} \approx -\mathbb{E}_t \left[R_{\mathcal{K}^*_*,t+1} - \frac{\operatorname{rer}_t}{\operatorname{rer}_{t+1}} R_{\mathcal{K}^*,t+1} \right]$$



INTEREST RATE UNCERTAINTY AS A POLICY TOOL



- Precautionary savings → Savings flow abroad where risk is lower (both bond and FDI)
- Rising markups (asymmetric profit): Inflationary pressure → Prices do not adjust to accommodate demand → Output ↓ → Demand for FDI ↓

INTEREST RATE UNCERTAINTY AS A POLICY TOOL



- Precautionary savings again but savings go to domestic investment
- No time-varying markups in producer prices: Take advantage of volatility if there are no frictions (Oi-Hartman-Abel effect) → Demand for incoming FDI ↑

INTEREST RATE UNCERTAINTY AS A POLICY TOOL



No time-varying markups in wages → Fall in R_K and R_{K*} is more pronounced (through factors of production) → Cut production → Cut input demand → Demand incoming FDI ↓

CONCLUSIONS

- Using domestic interest rate risk as a policy affects the composition of bond and FDI component of the current account
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Additional cases:

- Time-to-build FDI (against the policymaker)
- • LCP (in favor of the policymaker)
- Effective-lower-bound in the RoW (against the policymaker)
- Risk averse RoW investors (Epstein-Zin-Weil Preferences) (against the policymaker)

Firms

Intermediate Goods producers:

Producer Currency Pricing (PCP)

• Period profits:

$$rp_{H,t}(i) Y_{H,t}(i) + \left(\frac{1-n}{n}\right) rp_{H,t}^{*h}(i) Y_{H,t}^{*}(i) - mc_t \left(Y_{H,t}(i) + \left(\frac{1-n}{n}\right) Y_{H,t}^{*}(i)\right) - adj_{H,t} - adj_{H,t}^{*h}(i)$$

• Domestic and export demand:

$$Y_{H,t}(i) = \left(\frac{P_{H,t}(i)}{P_{H,t}}\right)^{-\epsilon} Y_{H,t}$$
$$Y_{H,t}^*(i) = \left(\frac{P_{H,t}^{*h}(i)}{S_t P_{H,t}^*}\right)^{-\epsilon} Y_{H,t}^*$$

FIRMS

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RESOURCE CONSTRAINTS

$$Y_t = C_t + I_t + I_t^* + adj_t^w + adj_t^{P_H} + adj_t^{P_H^{*h}}$$

$$Y_t^* = C_t^* + I_{*t}^* + I_{*t} + adj_t^{w^*} + adj_t^{P_t^*} + adj_t^{P_t^F}$$



MODEL OUTCOME WITH LEVEL SHOCKS



- Contractionary shock with national absorption
- Downward pressure on prices and wages

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- Introducing a time-to-build process for the FDI captures also irreversibility

• Law of motion of capital will be replaced by the following conditions:

$$\begin{split} & K_{*,t+1}(h) = (1-\delta) K_{*,t}(h) + I_{*,1,t}(h), \\ & I_{*,j-1,t+1}(h) = I_{*,j,t}(h); \qquad j = 2, \dots, J. \\ & I_{*,t}(h) = \sum_{j=1}^{J} \frac{1}{j} I_{*,j,t}(h) \end{split}$$

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• Notation:

 $\frac{1}{J}$: Fixed fraction of total investment expenditures allocated to projects that are *j* periods away from completion

 $I_{*,j,t}(h)$: Project that is initiated in period t and j periods away from completion.

Euler equation for Home capital that will be used in RoW and the respective pricing equation for the outgoing FDI:

$$q_{*,t+J-1} = \mathbb{E}_{t+J-1} \left[\beta_{t+J-1,t+J} \left(rer_{t+J} r_{K,*,t+J} + q_{*,t+J} \left(1 - \delta \right) \right) \right],$$
$$\mathbb{E}_{t} \left[\beta_{t,t+J-1} q_{*,t+J-1} \right] = \frac{1}{J} \left(rer_{t} + \mathbb{E}_{t} \left[\beta_{t,t+1} rer_{t+1} \right] + \dots + \mathbb{E}_{t} \left[\beta_{t,t+J-1} rer_{t+J-1} \right] \right).$$

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Current account:

$$\underbrace{(b_{t+1}-b_t) + \operatorname{rer}_t\left(b_{*,t+1}-b_{*,t}\right)}_{Bond\ component} + \underbrace{\frac{1}{J}\left[\left(\frac{1-n}{n}\right)\operatorname{rer}_t\left(K_{*,t+J}-K_{*,t}\right) - \left(K_{t+J}^*-K_{t}^*\right)\right]}_{FDI\ component} \equiv CA_t$$



Real options channel:

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 - Borrow from international markets to compensate the fall in consumption

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- Wait-and-see effects (Stokey, 2016)

Back to conclusion

- Baseline model: PCP
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- LCP: No inflation pass-through

The Rotemberg cost of adjusting the export price:

$$\left(\frac{1-n}{n}\right)\frac{\kappa^*}{2}\left(\frac{P_{H,t+s}^*(i)}{P_{H,t+s-1}^*(i)}-1\right)^2\frac{S_{t+s}P_{H,t+s}^*(i)}{P_{t+s}}Y_{H,t+s}^*.$$

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Relative price of Home output for domestic sales (*i.e.* $rp_H \equiv \frac{P_H}{P}$):

$$rp_{H,t} = \mu_{H,t}mc_t,$$

Relative price of Home output for export sales:

$$rp_{H,t}^* = \frac{\mu_{H,t}^* mc_t}{rer_t},$$



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- Precautionary savings channel still at work:
 - EME debt riskier \rightarrow Short-term outflows

Time-to-build and LCP

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 - Trade-offs between smoothing across states vs. smoothing across time
- What are the implications when RoW agents are more risk averse?

Generalize expected discounted sum of utility to:

$$V_t \equiv (1-\beta) U(C_t(h), L_t(h)) - \beta \left[\mathbb{E}_t \left(-V_{t+1} \right)^{1-\alpha} \right]^{1/(1-\alpha)}$$

• When $\alpha = 0$, it reduces to the standard utility as before

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The discount factor of RoW agents, $\beta_{t,t+1}^*$, becomes

$$\beta_{t,t+1}^{*} \equiv \frac{\beta U_{C,t+1}^{*}}{U_{C,t}^{*}} \left(\frac{-V_{t+1}^{*}}{\left(\mathbb{E}_{t} \left[-V_{t+1}^{*1-\alpha^{*}} \right] \right)^{1/(1-\alpha^{*})}} \right)^{-\alpha^{*}}$$

- Additional term reflecting the early resolution of uncertainty
- With α* < 0, unfavorable changes in utility imply a higher discount factor for RoW agents



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 - ▶ Hike in prices \rightarrow Lower rental rates \rightarrow RoW agents cut their investment
- International comovement in consumption → RoW consumption ↓ and RoW savings ↑
- Amplified precautionary savings channel imply a more pronounced appreciation in RER (from EME perspective)
 - EME risk premium $\uparrow \rightarrow$ Short-term inflows \uparrow

$$R_t - R_t^* \approx \mathbb{E}_t \Delta s_{t+1} + \underbrace{\frac{1}{2} Var_t(\Delta s_{t+1}) + Cov_t(\beta_{t+1}^*, \Delta s_{t+1})}_{=\frac{1}{2} Var_t(\beta_{t+1}^*) - \frac{1}{2} Var_t(\beta_{t+1})}$$

Back to conclusion

STOCHASTIC STEADY STATE: ILLUSTRATION

Figure: Accumulation decision function in a linearized model and in a nonlinear model



- When accumulation function is concave, at the deterministic steady-state, accumulation will be greater than in absence of risk due to precautionary motive.
- It is point C that defines stochastic steady state.

Back to what we do

• Third-order approximation of the model is needed to single out the individual effects of volatility shocks

- Third-order approximation of the model is needed to single out the individual effects of volatility shocks
- Solutions using higher-order perturbation techniques tend to yield explosive time-paths due to accumulation of terms higher-order
 - Pruning all higher-order terms (Andreasen et alii (2013))

Simulated paths of states and controls move away from their non-stochastic steady-state values.

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- Starting from the ergodic mean in the absence of shocks, hit the model with a 2 std deviation shock to the volatility process, ε_t^{σ}
- Calculate IRFs as deviation from the ergodic mean in the absence of shocks
- Back to presentation

Illustration of the Stochastic Steady State

CALIBRATION

Parameter		Value	Comments
Discount factor	β	0.9804	2% Real Rate
Relative risk aversion	ρ	2	Literature
Relative weight of labor in utility	X	1	Literature
Frisch elasticity	φ	0.25	Literature
Deposit adjustment	ψ	0.0025	Literature
Rotemberg wage adjustment	κ ^W	116	\approx 3 period stickiness
Elas. of substitution of differentiated labor	ϵ^W	11	Wage markup of 10%
Home bias	а	.65	Unsal (2013)
Share of domestic capital	α_1	.30	ABK (2016)
Share of foreign capital	α_2	0.15	ABK (2016)
Rotemberg domestic price adj.	к	116	\approx 3 period stickiness
Rotemberg export price adj.	κ*	116	\approx 3 period stickiness
Elas. of substitution in goods production	ϵ	11	Price markup of 10%
Smoothing coefficient	ρ_R	0.7	Literature
SS response to inflation	$ ho_\Pi$	1.5	Literature
SS response to output	ρ_Y	0.5/4	Literature

MODEL OUTCOME WITH LEVEL SHOCK



TIME-TO-BUILD COMPARISON



▶ Back

TIME-TO-BUILD COMPARISON





EFFECTIVE-LOWER-BOUND IN THE ROW



EFFECTIVE-LOWER-BOUND IN THE ROW (HIGH HOME BIAS)

