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**Comparison of Various Fiscal Policies in the Face of Different
Demographic Stages**

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Abstract

This study examines the impact of aging on the effectiveness of various fiscal expenditures, including government consumption, one-time government transfers to households, public investment, and R&D spending, using a dynamic stochastic general equilibrium model. Our findings reveal that (1) Aging enhances the effects of the transfer on augmenting GDP. (2) Regardless of aging, R&D expenditure consistently stands out over all time spans, with younger society benefiting more. (3) Public investment ranks second among 4 different fiscal policies compare in the long run while younger society shows bigger impact. (4) Government consumption has only a temporary effect and is the least effective in boosting GDP in both young and old societies. (5) Multipliers for public investment and R&D expenditure increase with the accumulation of public capital and TFP. The multipliers of young society is larger than old society because impact on consumption is much more effective.

Keywords: Fiscal Policy Effectiveness, Aging Population, Japan, DSGE Model.

JEL Code: E62, H30, J1

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1. Introduction

Population aging presents a significant challenge for policymakers across both developed and developing countries (Figure 1). Recent studies have thus explored the link between population aging and the effectiveness of fiscal spending. Honda and Miyamoto (2021) found that aging reduces the output-enhancing effects of fiscal expenditure in OECD countries during recessions. Similarly, Basso and Rachedi (2021) identified larger fiscal multipliers in U.S. states characterized by younger populations. Miyamoto and Yoshino (2022) found that aging diminishes the impact of fiscal stimulus on private consumption and employment.¹

Despite these insights, there remains a significant gap in understanding how aging influences the outcome of various fiscal measures. Moreover, the literature has yet to fully explore the heterogeneity in the effects of different fiscal expenditures. A critical oversight is the lack of detailed analysis regarding in the underlying mechanisms through which population aging impacts these fiscal measures

Addressing these gaps, this paper compares various fiscal policies facing different stages of demography using a dynamic stochastic general equilibrium (DSGE) model that includes both workers and retirees, developed by Yoshino and Miyamoto (2017).² We offer three key expansions: First, we thoroughly investigate how aging influences the macroeconomic effectiveness of fiscal expenditures. Second, we compare a wide range of fiscal policies, including (i) government consumption aimed at stimulating aggregate demand, (ii) universal government transfers to all generations, (iii) public investment in infrastructure, and (iv) R&D expenditure fostering technological progress. The first two policies primarily aim to stimulate aggregate demand in the economy, while the

¹ In the context of Japan, Bessho (2021) demonstrated higher fiscal multipliers in regions with younger populations.

² As Yoshino and Le (2022) shows, analysis of aging using an overlapping generations (OLG) model is possible, demonstrating the potential for a decline in the effectiveness of fiscal and monetary policies. However, akin to Yoshino and Miyamoto (2017), introducing heterogeneous agents into a DSGE model, accommodating both workers and the elderly simultaneously, allows for an analysis of policy in scenarios where the proportion of the elderly changes. Thus, we argue that the method utilized in this paper is superior to OLG.

1 latter two contribute to enhancing aggregate supply.

2 The results of our policy simulation are summarized as follows: Firstly, the
3 GDP-enhancing effect of the three policies (namely, government consumption,
4 government investment and R&D expenditures), other than one-time
5 government transfer, decreases with aging. Aging implies an increase in the
6 share of policy-irrelevant, stable consumption among retirees in aggregate
7 consumption, thereby weakening the demand expansion effect of the three
8 policies other than one-time transfers. Meanwhile, the output multiplier effect
9 of the transfer gives a greater demand expansion effect with aging due to a larger
10 increase in the sum of retirees' consumption. Secondly, regardless of the degree
11 of aging, R&D expenditure consistently emerges as the most effective measure
12 across all time spans due to its considerable impact on aggregate supply. Public
13 investment ranks second in the long run, while government consumption takes
14 this position in the short run. The one-time transfer is the least effective in
15 expanding GDP in any time spans except for the very short term. Thirdly,
16 government consumption multipliers tend to decrease over time after policy
17 implementation, indicating stronger short-term stimuli but weaker long-term
18 effects. These time-dependent changes in fiscal multipliers become more
19 pronounced as aging progresses. Moreover, the rank of fiscal policies' welfare
20 multiplier aligns with the output multiplier. Furthermore, demographic aging
21 significantly diminishes the welfare benefits from policies enhancing aggregate
22 supply, underscoring the need for nuanced policy considerations in the face of
23 shifting demographic structures.

24 The paper proceeds as follows: Section 2 extends the New Keynesian
25 model with retired workers. Section 3 calibrates the model. Section 4 examines
26 fiscal policies' impacts. Section 5 compares various fiscal policies in face of
27 different demographic stages. Section 6 presents conclusions.

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(Figure 1 around here)

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32 **2. The Model**

33

34 Our model consists of four sectors: households, firms, government, and

1 central bank. Households are conceptualized as a continuum distributed over
2 the interval $[0,1]$. Within this framework, a proportion ϕ of households is
3 characterized as workers, while the rest represents retirees. In addition to
4 heterogeneous households, our model incorporates monopolistic competition
5 and price stickiness among firms, following Calvo (1983). The government
6 operates under a budget constraint, collecting revenue through lump-sum taxes
7 and influencing the economy through various fiscal spendings. The central bank
8 balances inflation and economic growth stability by controlling the nominal
9 interest rate.

10 As our model's household and firm settings are similar to those of Yoshino
11 and Miyamoto (2017), we focus on describing the main modifications here. By
12 changing elderly ratio we can analyze the impact of various fiscal policies in
13 young economy.

14 2.1 Household's Problem

15 We begin with the worker's problem. In the standard New Keynesian model,
16 government consumption is wasteful expenditure, crowding out private
17 consumption through a negative wealth effect. However, many empirical
18 studies on macro-data in Japan have ascertained that an increase in government
19 consumption positively influences private consumption (see, for instance,
20 Kameda, 2014; Morita, 2015). To better reconcile with this finding, Yoshino and
21 Miyamoto (2017) introduces imperfect substitutability between private and
22 government consumption in households' utility function. Consequently, the
23 expected lifetime utility function of a worker is given by

$$24 \quad \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \left\{ \frac{1}{1-\sigma} \left[\left\{ \omega c_{w,t}^{\frac{\zeta-1}{\zeta}} + (1-\omega) g_t^{\frac{\zeta-1}{\zeta}} \right\}^{\frac{\zeta}{\zeta-1}} \right]^{1-\sigma} - \frac{h_{w,t}^{1+\mu}}{1+\mu} \right\} \quad (1)$$

25 where $\beta \in (0,1)$ is subjective discount factor, $c_{w,t}$ is one worker's consumption,
26 g_t is government consumption of such services as hospital service, free public
27 transportation, etc., and $h_{w,t}$ is work hours. The parameter $1/\sigma$ is intertemporal
28 elasticity of substitution, and $1/\mu$ is the Frisch elasticity of labor supply. The
29 parameter ζ is the elasticity of substitution between private and government
30 consumption, and the share parameter ω determines how much government
31 consumption affects utility.
32
33

1 The budget constraint of a worker is as follows:

$$2 \quad c_{w,t} + i_{w,t} + b_{w,t} = w_t h_{w,t} + r_t k_{w,t-1} + R_{t-1} \frac{b_{w,t-1}}{\pi_t} + d_{w,t} - \tau_{w,t} + TR_{w,t} \quad (2)$$

3 where w_t is real wages, r_t is the real interest rate, R_t is the gross nominal
4 interest rate, $d_{w,t}$ is the dividend that the worker receives from the firm sector,
5 $\tau_{w,t}$ is the lump-sum tax, $TR_{w,t}$ is the one-time transfer received by workers,
6 and $\pi_t \equiv P_t/P_{t-1}$ is the gross inflation rate.

7 The accumulation of one worker's capital stock is given by

$$8 \quad k_{w,t} = (1 - \delta)k_{w,t-1} + i_{w,t} \quad (3)$$

9 where δ is the depreciation rate and $i_{w,t}$ is investment of one worker.

10 The worker chooses consumption $c_{w,t}$, capital stock $k_{w,t}$, and government
11 bonds $b_{w,t}$ to maximize the above expected lifetime utility subject to the budget
12 constraint and capital accumulation equation. The first-order conditions are as
13 follows:

$$14 \quad \left(\omega c_{w,t}^{\frac{\zeta-1}{\zeta}} + (1 - \omega) g_t^{\frac{\zeta-1}{\zeta}} \right)^{\frac{1-\sigma\zeta}{\zeta-1}} \omega c_{w,t}^{\frac{-1}{\zeta}} = \lambda_t \quad (4)$$

$$15 \quad h_{w,t}^\mu = \lambda_t w_t \quad (5)$$

$$16 \quad \beta \mathbb{E}_t \lambda_{t+1} [r_{t+1} + 1 - \delta] = \lambda_t \quad (6)$$

$$17 \quad \beta \mathbb{E}_t \frac{\lambda_{t+1} R_t}{\pi_{t+1}} = \lambda_t \quad (7)$$

18 where λ_t is the Lagrange multiplier on the budget constraint, which also
19 represents the worker's marginal utility of income.

20 The remaining measure of $1 - \phi$ households is retired. The lifetime utility
21 function of a retiree is given by

$$22 \quad \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \frac{1}{1 - \sigma} \left[\left\{ \omega c_{r,t}^{\frac{\zeta-1}{\zeta}} + (1 - \omega) g_t^{\frac{\zeta-1}{\zeta}} \right\}^{\frac{\zeta}{\zeta-1}} \right]^{1 - \sigma} \quad (8)$$

23 where $c_{r,t}$ is one retiree's consumption.

24 Following Yoshino and Miyamoto (2017), retirees are not confronted with
25 the trade-off between saving and consumption. Nevertheless, considering the
26 uniformity of pension disbursements over time and anchored in the principle of
27 consumption smoothing, it follows logically that a retiree's optimal
28 consumption mirrors the pension they receive. Thus, the consumption of one
29 retiree $c_{r,t}$ is

1
$$c_{r,t} = s \times \bar{w} + TR_{r,t} \quad (9)$$

2 where $s \times \bar{w}$ is the pension related to the steady state value of real wages.
 3 Moreover, $TR_{r,t}$ is the one-time transfer received by retirees.

4

5 **2.2 Firm's Problem**

6 As we explained earlier, there are two types of firms: a perfectly competitive
 7 final good firm and monopolistic competitive intermediate goods firms indexed
 8 by $j \in [0,1]$. No corporate tax is considered for simplicity.

9 The final good Y_t is produced by combining a continuum of differentiated
 10 intermediate goods $y_{j,t}$. The production function is given by

11
$$Y_t = \left(\int_0^1 y_{j,t}^{\frac{\epsilon-1}{\epsilon}} dj \right)^{\frac{\epsilon}{\epsilon-1}} \quad (10)$$

12 where ϵ governs the degree of substitution between different inputs.

13 The final good producer is perfectly competitive and maximizes real profits
 14 subject to (10). Thus, the problem of the final good producer is

15
$$\max_{y_{j,t}} P_t Y_t - \int_0^1 P_{j,t} y_{j,t} dj \quad (11)$$

16 This yields the demand for intermediate goods:

17
$$y_{j,t} = \left(\frac{P_{j,t}}{P_t} \right)^{-\epsilon} Y_t \quad (12)$$

18 Substituting (12) into (10), we have the following relationship between the
 19 aggregate price level and the prices of intermediate goods:

20
$$P_t^{1-\epsilon} = \int_0^1 (P_{j,t})^{1-\epsilon} dj \quad (13)$$

21 The production function of intermediate goods firm j is given by

22
$$y_{j,t} = A_t (k_{j,t-1})^\alpha (h_{j,t})^{1-\alpha} k_{g,t}^{\alpha_g}, \quad 0 < \alpha < 1, \quad 0 < \alpha_g < 1 \quad (14)$$

23 where $k_{j,t-1}$, $k_{g,t}$ and $h_{j,t}$ represent private capital, aggregate public capital and
 24 labor services hired by firm j , and A_t denotes the TFP. Public capital is treated
 25 as exogenous for simplicity.

26 Cost minimization implies

27
$$\frac{k_{j,t-1}}{h_{j,t}} = \frac{\alpha w_t}{(1-\alpha)r_t} \quad (15)$$

1 This equation implies that the capital-labor ratio is equalized across
 2 intermediate goods producers. Then, the marginal costs of firms are given by

$$3 \quad mc_t = \frac{r_t^\alpha w_t^{1-\alpha}}{A_t k_{g,t}^{\alpha_g}} \quad (16)$$

4 We assume that intermediate goods firms are subject to price setting frictions
 5 à la Calvo (1983). Thus, an intermediate goods firm can set its price optimally
 6 with probability $1-\xi$, and with probability ξ , it must keep its price unchanged
 7 relative to what it was in the previous period:

$$8 \quad P_{j,t} = P_{j,t-1}. \quad (17)$$

9 A firm optimizing its price maximizes

$$10 \quad \max_{P_{j,t}^*} \mathbb{E}_t \sum_{i=0}^{\infty} (\beta\xi)^i \lambda_{t+i} \{P_{j,t}^* - P_{t+i} mc_{t+i}\} y_{j,t+i} \quad (18)$$

11 subject to the demand function

$$12 \quad y_{j,t+i} = \left(\frac{P_{j,t}^*}{P_{t+i}} \right)^{-\epsilon} Y_{t+i}, \quad (19)$$

13 and where P_t^* is the optimal nominal price.

14 The profit maximization problem yields

$$15 \quad P_{j,t}^* = \frac{\epsilon}{\epsilon-1} \frac{\mathbb{E}_t \sum_{i=0}^{\infty} (\beta\xi)^i \lambda_{t+i} mc_{t+i} y_{j,t+i}}{\mathbb{E}_t \sum_{i=0}^{\infty} (\beta\xi)^i \lambda_{t+i} \frac{y_{j,t+i}}{P_{t+i}}} \quad (20)$$

16 Finally, combine with Eq. (13), the law of motion for the aggregate price level
 17 is given by

$$18 \quad P_t = [\xi P_{t-1}^{1-\epsilon} + (1-\xi) P_{j,t}^{*1-\epsilon}]^{\frac{1}{1-\epsilon}}. \quad (21)$$

19

20 **2.3 Aggregation of the economy**

21 The aggregate level of any consumer-specific variables $x_{i,t}$ where $i \in \{w, r\}$

22 is given by $x_t = \int_0^1 x_{i,t} di = \phi x_{w,t} + (1-\phi)x_{r,t}$, as households in each of the

23 two groups are identical. Hence, aggregate consumption c_t is given by

$$24 \quad c_t = \phi c_{w,t} + (1-\phi) c_{r,t}. \quad (22)$$

1 Since only workers provide labor services and retirees keep constant real
 2 deposits (capital stock), the aggregate hours of worker h_t , aggregate capital
 3 supply k_t , and aggregate investment i_t are given by

$$4 \quad h_t = \phi h_{w,t} \quad (23)$$

$$5 \quad k_t = \phi k_{w,t} \quad (24)$$

$$6 \quad i_t = \phi i_{w,t} \quad (25)$$

7 We assume that the one-time transfer payments for retirees and workers are
 8 identical. Consequently, the aggregated transfer payments can be expressed as:

$$9 \quad TR_t = \phi TR_{w,t} + (1 - \phi) TR_{r,t}, \quad TR_{w,t} = TR_{r,t} \quad (26)$$

10 Similarly, only workers hold financial assets, receive dividends from firms,
 11 and pay the lump-sum tax. Thus, we have

$$12 \quad b_t = \phi b_{w,t} \quad (27)$$

$$13 \quad d_t = \phi d_{w,t}, \quad (28)$$

$$14 \quad \tau_t = \phi \tau_{w,t}. \quad (29)$$

15 In this paper, policy effects in different aging economy will be compared
 16 by changing the value of ϕ in Section 5.

17 2.4 Fiscal and Monetary Authorities

18
 19 The government purchases goods for consumption g_t , public investment
 20 purpose $i_{g,t}$, R&D expenditure for technology RD_t , social security benefits
 21 $(1 - \phi)s\bar{w}$, and one-time transfer TR_t . It finances them by levying the lump-
 22 sum tax and issuing government bonds. Hence, the government budget
 23 constraint in real terms is given by

$$24 \quad b_t + \tau_t = g_t + i_{g,t} + R_{t-1} \frac{b_{t-1}}{\pi_t} + (1 - \phi)s \times \bar{w} + TR_t + RD_t. \quad (30)$$

25 The accumulation of public capital follows:

$$26 \quad k_{g,t} = i_{g,t} + (1 - \delta)k_{g,t-1} \quad (31)$$

27 Public investment $i_{g,t}$ follows a stochastic process:

$$28 \quad \log(i_{g,t}) = (1 - \rho_{ig}) \log(\bar{i}_g) + \rho_{ig} \log(i_{g,t-1}) + \epsilon_{ig,t}, \quad \epsilon_{ig,t} \sim N(0, \sigma_{ig}^2).$$

$$29 \quad (32)$$

1 Government consumption g_t follows a stochastic process:

$$2 \quad \log(g_t) = (1 - \rho_g)\log(\bar{g}) + \rho_g\log(g_{t-1}) + \epsilon_{g,t}, \quad \epsilon_{g,t} \sim N(0, \sigma_g^2). \\ 3 \quad (33)$$

4 Similarly, the one-time transfer follows:

$$5 \quad \log(TR_t) = (1 - \rho_{tr})\log(\overline{TR}) + \rho_{tr}\log(TR_{t-1}) + \epsilon_{tr,t}, \quad \epsilon_{tr,t} \sim N(0, \sigma_{tr}^2). \\ 6 \quad (34)$$

7 For representing the effect of R&D expenditure RD_t , we specify that the
8 TFP follows the stochastic process below³.

$$9 \quad \log(A_t) = \rho_a\log(A_{t-1}) + \rho_{ag}\left(\frac{RD_t}{Y_t} - \frac{\overline{RD}}{\overline{Y}}\right) + \epsilon_{a,t}, \quad \epsilon_{a,t} \sim N(0, \sigma_a^2) \\ 10 \quad (35)$$

11 Moreover, the R&D expenditure shock takes the following form:

$$12 \\ 13 \quad \log(RD_t) = \rho_{RD}\log(RD_{t-1}) + (1 - \rho_{RD})\log(\overline{RD}) + \epsilon_{RD,t}, \quad \epsilon_{RD,t} \sim N(0, \sigma_{RD}^2) \\ 14 \quad (36)$$

15 where ρ_{RD} is the persistency of R&D expenditure shock.

16 Furthermore, we allow for debt financing but assume a tax rule exists to
17 keep the level of real debt constant in the long run. Thus, the tax rule is

$$18 \quad \frac{\tau_t}{\bar{\tau}} = \left(\frac{b_{t-1}}{\bar{b}}\right)^\psi, \quad (37)$$

19 where ψ is the feedback parameter from debt to taxes. The monetary policy
20 follows a Taylor rule,

$$21 \quad \frac{R_t}{\bar{R}} = \left(\frac{\pi_t}{\bar{\pi}}\right)^{\varphi_\pi} \left(\frac{Y_t}{\bar{Y}}\right)^{\varphi_Y} \exp(\nu_t), \quad (38)$$

³ In the second term of equation (33), we adjust the ratio of R&D expenditure to GDP by subtracting its steady-state value, ensuring that TFP eventually converges to its steady-state level. This adjustment is crucial for ensuring that the model possesses a well-defined steady state without growth trend, following Minford and Meenagh (2019).

1 where any variable without a time subscript denotes the corresponding steady-
 2 state value of the variable, φ_π Indicates how strongly the monetary authority
 3 responds to deviations of inflation from target, φ_Y is the response to the output
 4 gap, and v_t follows a stochastic process:

$$5 \quad v_t = \rho_\nu v_{t-1} + \varepsilon_{\nu,t}, \varepsilon_{\nu,t} \sim N(0, \sigma_\nu^2). \quad (39)$$

6

7 **2.5 Market Clearing Conditions**

8 The labor market is in equilibrium when the labor demand by the intermediate
 9 goods firms $h_t \equiv \int_0^1 h_{j,t} dj$ is equal to the labor services supplied by workers.

10 Similarly, the capital rental market is in equilibrium when the demand for capital
 11 by the intermediate goods firms $k_t \equiv \int_0^1 k_{j,t} dj$ equals to the capital supply. The

12 monetary policy rule determines the nominal interest rate. In order to maintain
 13 money market equilibrium, the money supply adjusts endogenously to meet the
 14 money demand at those interest rates. The final good market is in equilibrium
 15 when the supply by the final good firms (Eq. 10) equals the demand by
 16 consumers and the government:

$$17 \quad Y_t = c_t + i_t + g_t + RD_t + i_{g,t} \quad (40)$$

18

19 **3. Calibration for quarterly macroeconomic data**

20

21 Calibrating the model, we utilize Japanese data, which reflects the most
 22 pronounced aging trends worldwide, as summarized in Table 1. The model
 23 period is set to one quarter, with a subjective discount factor of $\beta = 0.99$,
 24 implying a 4% per year steady-state real interest rate.

25 Following existing studies, we calibrate parameters in the consumer utility
 26 function. We set the risk aversion parameter $\sigma = 1.0$ following the estimation
 27 of Sugo and Ueda (2008). In addition, μ is set at 2.0 indicating a Frisch elasticity
 28 of $1/\mu = 0.5$, in line with micro evidence (Kuroda and Yamamoto, 2008). We
 29 set the share parameter of public and private goods $\omega = 0.6$ and elasticity of
 30 substitution $\zeta = 0.4$ based on Hamori and Asako (1999) and Brückner and

1 Pappa (2012).

2 Turning to the production function, we target capital share with $\alpha=1/3$ and
3 normalize the steady state of technology level to $\bar{A} = 1$. Based on the estimation
4 of Kameda et al. (2022), we set the elasticity of output with respect to public
5 capital $\alpha_g = 0.2$. We set the depreciation rate $\delta = 0.028$ following Esteban-
6 Pretel et al. (2010).

7 Next, we calibrate nominal rigidity parameters based on existing studies.
8 Specifically, demand elasticity is set to $\epsilon = 11$, implying a steady-state markup
9 of 10%. Considering estimates from Iiboshi et al. (2006), Sugo and Ueda (2008),
10 Ichiue et al. (2013), and Kuo and Miyamoto (2016), we set the Calvo parameter
11 to $\xi = 0.8$, indicating an average contract duration of approximately five
12 quarters.

13 We determine the fraction of workers ϕ based on the ratio of the population
14 aged 20–64 to those aged 20 or older, setting $\phi = 0.85$ according to the
15 National Institute of Population and Social Security Research.

16 As for policy parameters, to maintain comparability with existing studies
17 (Clarida et al. 1998; Fujiwara et al. 2007; Fujiwara et al. 2008) we set $\varphi_\pi = 1.5$
18 and $\varphi_Y = 0.1$ for the Taylor rule.

19 Based on relevant surveys, Explanation of the Statistical Survey of Actual
20 Status for Salary in the Private Sector conducted by the National Tax Agency,
21 and the Annual Report on the Public Pension System conducted by the Ministry
22 of Health, Labour and Welfare, we set the ratio of average pensions to average
23 salary s to 0.4. Additionally, we establish steady-state values for the
24 government spending to GDP ratio ($\bar{g}/\bar{Y} = 0.16$), one-time transfer to GDP
25 ratio ($\bar{TR}/\bar{Y} = 0.03$), public investment to GDP ratio ($\bar{I}_g/\bar{Y} = 0.06$) and debt to
26 GDP ratio ($\bar{b}/\bar{Y} = 1.7$), following Yoshino and Miyamoto (2017). The steady-
27 state value for R&D expenditure to GDP ratio \bar{RD}/\bar{Y} is set to 0.04 based on data
28 of Chun et al. (2012). Following Kato and Miyamoto (2013), we set government
29 spending autoregressive parameters $\rho_g = \rho_{RD} = \rho_{tr} = 0.9$, the same as each
30 other for comparison. Lastly, following Gali et al. (2007), we consider a
31 moderately persistent monetary shock and set $\rho_v = 0.5$.

32 Furthermore, we calibrate the persistency parameter of TFP, ρ_a , and the
33 elasticity of TFP with respect to R&D expenditure ρ_{ag} through an empirical
34 study for Japan as follows. Chun et al. (2012) estimates the relationship between

1 the growth rate of TFP and R&D expenditure as follows:

$$2 \quad d \log(A_t) = \beta_1 \frac{RD_t}{Y_t} + \beta_2 \log(A_{t-1})$$

3 where β_1 and β_2 is estimated as 0.61 and -0.13 , respectively. We can re-
4 write this regression equation as follows:

$$5 \quad \log(A_t) = \beta_1 \frac{RD_t}{Y_t} + (1 + \beta_2) \log(A_{t-1})$$

6 Therefore, we can calibrate the values of ρ_a and ρ_{ag} to match the stochastic
7 process of TFP in Eq. (33) with this regression equation.

$$8 \quad \begin{cases} \rho_a = 1 + \beta_2 = 0.87 \\ \rho_{ag} = \beta_1 = 0.61 \end{cases}$$

9 Overall, our calibration is based on existing studies and statistical data, and
10 we believe it provides a reasonable representation of the Japanese economy.

11 Finally, drawing on the approach used by Yoshino and Miyamoto (2017),
12 we set the labor participation rates ϕ at 0.85 and 0.55 respectively, to simulate
13 the effects on fiscal policy. This method allows for a nuanced understanding of
14 how changes in population structure can influence macroeconomic dynamics
15 after the implication of fiscal policies. With a labor participation rate $\phi = 0.85$,
16 we set the debt-to-taxes feedback parameter ψ to 0.1 following Mayer et al.
17 (2010). To maintain consistent tax revenues across different population
18 structures, we adjust ψ to 0.067 when $\phi = 0.55$. This change only affects the
19 dynamics of lump-sum taxes and national debt, with no impact on other
20 variables.

21 Table 1: Parameter values (quarterly basis)

Parameter	Description	Value	Source/Target
β	Discount factor	0.99	Data
σ	Relative risk aversion parameter	1.0	Sugo and Ueda (2008)
μ	The inverse of Frisch elasticity	2.0	Kuroda and Yamamoto (2008)
ω	Share parameter of government consumption	0.6	Hamori and Asako (1999)
ζ	Elasticity of utility function	0.4	Brückner and Pappa (2012)
α	Capital share	1/3	Data
α_g	Elasticity of output with respect to public capital	0.2	Kameda et al. (2022)
\bar{A}	Steady state of aggregate	1.0	Normalization

	productivity		
δ	Depreciation rate	0.028	Esteban-Pretel et al. (2010)
ϵ	Elasticity of demand	11	10% steady-state markup rate
ξ	Calvo parameter	0.8	Kuo and Miyamoto (2016)
ϕ	Fraction of workers	0.85	Data
φ_y	Taylor rule coefficient for output	0.1	Fujiwara et al. (2008)
φ_π	Taylor rule coefficient for inflation	1.5	Fujiwara et al. (2008)
ψ	Feedback parameter in the tax rule	0.1 and 0.067	Mayer et al. (2010)
s	Social security benefits to wage ratio	0.4	Annual Report on the Public Pension System
\bar{g}/\bar{Y}	Government spending to GDP ratio	0.16	Yoshino and Miyamoto (2017)
\overline{TR}/\bar{Y}	One-time transfer to GDP ratio	0.03	Yoshino and Miyamoto (2017)
\bar{i}_g/\bar{Y}	Public investment to GDP ratio	0.06	Yoshino and Miyamoto (2017)
\bar{b}/\bar{Y}	Debt to GDP ratio	1.7	Yoshino and Miyamoto (2017)
\overline{RD}/\bar{Y}	R&D expenditure to GDP ratio	0.06	Chun et al. (2012)
ρ_g	Persistence of gov. consumption shock	0.9	Kato and Miyamoto (2013)
ρ_v	Persistence of monetary policy shock	0.5	Gali et al. (2007)
ρ_{tr}	Persistence of one-time transfer	0.9	Kato and Miyamoto (2013)
ρ_{RD}	Persistence of gov. R&D expenditure shock	0.9	Kato and Miyamoto (2013)
ρ_a	Persistence of TFP	0.87	Chun et al. (2012)
ρ_{ag}	Elasticity of TFP with respect to R&D expenditure	0.61	Chun et al. (2012)
ϕ	Labor participant ratio	0.85 and 0.55	Yoshino and Miyamoto (2017)

1

2

3 4. Quantitative Analysis

4

5 This section will consider how aging change the macroeconomic effects of
6 the four types of government fiscal policies, i.e., government consumption on
7 public goods, g_t , universal one-time government transfers to all generations,
8 TR_t , public investment in infrastructure $i_{g,t}$, and the R&D expenditure
9 augmenting TFP, RD_t .

10 In the steady state, the ratios of the four fiscal expenditures to GDP vary, as

1 shown in Table 1. When applying a 1% policy shock to each, the actual increase
2 in expenditure differs for each type. For example, a 1% shock in government
3 consumption leads to a 0.16% rise in the GDP's steady state value. In contrast,
4 a 1% one-time transfer shock results in only a 0.03% rise. So, it's not accurate
5 to compare these policies by just using a 1% shock. To make a fair comparison,
6 we adjust the shock size so that the initial increase in each expenditure type is
7 equal to 0.01% of the GDP's steady-state value.

8 Before the comparison, we show the impulse responses to a 0.01% GDP
9 increase in government consumption, assuming no complement effects with
10 private consumption in Figure 2 as a benchmark.⁴ These responses, as expected,
11 closely resemble the outcomes in the standard Real Business Cycle model. The
12 anticipated future tax burden on workers triggers a negative wealth effect,
13 leading to a reduction in their consumption. This effect, in turn, raises labor
14 supply and savings. However, the rise in government consumption outweighs
15 the decrease in private consumption, thereby boosting aggregate demand. In the
16 capital market, the additional national debt absorbs households' savings,
17 diminishing the supply of productive capital. Despite this, the expansion of
18 aggregate demand increases capital demand, overwhelming the supply.
19 Consequently, the real interest rate rises, and private investment is crowded out.
20 In the labor market, the increase in labor supply exceeds the heightened labor
21 demand, causing a decline in real wages. In a parameter setting reflecting the
22 Japanese economy, the increased real interest rate and decreased real wage lead
23 to a rise in the marginal cost of intermediate goods for firms, resulting in an
24 increase in the inflation rate. Furthermore, the central bank raises the nominal
25 interest rate through the Taylor rule.

26 Following the initial shock, the increment of government consumption
27 declines. However, the accumulation of debt continued, leading to a sustained
28 rise in real interest rate. Consequently, the marginal costs and inflation rates also
29 increases, along with nominal interest rates. Also, this increase in real interest
30 rate decreases the labor supply through factor substitution, which makes wage
31 recovers to its steady state.

⁴ In this case, we set the share parameter, ω , for private consumption in the utility function to 1. Consequently, government consumption does not augment the marginal utility of private consumption and becomes a kind of 'wasteful expenditure'.

1 Let us now examine the effects of aging on this fiscal spending, comparing
2 macroeconomic responses under two different demographic structures, $\phi =$
3 0.85 and 0.55. Given the complexity of causal mechanisms involved, we
4 categorize these effects into two components: the demand-side aging effect and
5 the supply-side aging effect.

6 On the demand-side, aging works to weaken the policy effects. Aggregate
7 consumption consists of the weighted sum of workers' and retirees'
8 consumption. An increase in government expenditure decreases workers'
9 consumption through the negative wealth effects. Meanwhile, aging means a
10 decrease in the share of workers in total population. Under our parameter
11 settings, this decreased share effects overwhelms the negative wealth effects.
12 Therefore, aging reduces the increase in aggregate consumption that
13 government aims to expand. We call this mitigation effect of aging “the demand-
14 side aging effect.” Note that retirees are characterized by their Rule-of-Thumb
15 behavior but shielded from the volatility of labor income due to their stable
16 pension incomes.⁵

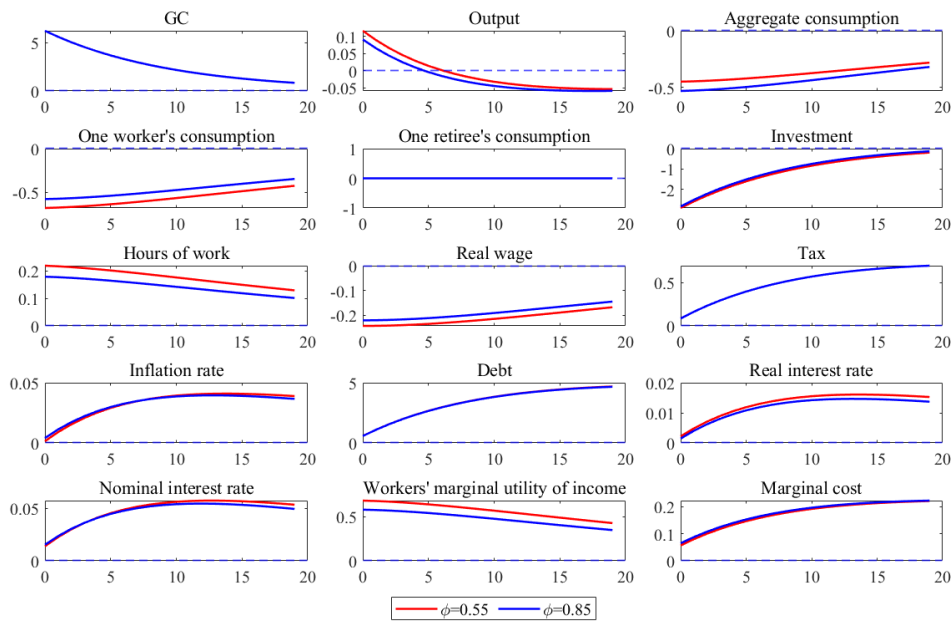
17 On the other hand, aging concentrates the tax burden on a smaller amount
18 of workers. Therefore, when the government increases fiscal expenditure in the
19 aging economy, the resultant reduction in workers' lifetime income amplifies
20 the increase in factor supply: labor supply and saving. We refer to this factor-
21 increasing effects as “the supply-side aging effect.”

22 Based on these two-side effects, let us consider the total aging effect. When
23 the government expands their consumption in an aging economy ($\phi = 0.55$),
24 aging works to mitigate the policy effect through the demand-side aging effects,
25 resulting in a smaller decrease in aggregate consumption. As evident, this leads
26 to a greater increase in aggregate demand, and subsequently, in labor and capital

⁵ This setting is different from Gali et al. (2007), which also introduced a segment of households—those adhering to the Rule-of-Thumb consumption behavior—into their model. These households do not save and thus their consumption is equal to their labor income. Gali et al. (2007) reported that an increase in government consumption not only elevates the labor income of these Rule-of-Thumb households but also intensifies the positive repercussions on aggregate consumption and output.

1 demand. On the other hand, the supply-side effects are amplified by aging,
 2 resulting in a greater increase in factor supply. In the labor market, the supply
 3 overwhelms the demand; therefore, the real wage is lower than in the case of
 4 $\phi = 0.85$. In contrast, real interest rates become higher in the capital market.
 5 Under our parameter setting, the changes in factor prices does not change the
 6 marginal cost of intermediate good for firms, thereby have a little influence in
 7 the inflation rate and nominal interest rate

8
 9



10

11 Figure 2: Impulse responses to a 0.01% increase of GDP in government
 12 consumption without complimentary effect
 13 (Basis point deviation from steady state values)

14

15 Note: Impulse responses reflect basis point deviations from steady-state values.
 16 Red lines labeled “ $\phi=0.85$ ” show responses from the model with higher labor
 17 participation, while blue lines labeled “ $\phi=0.55$ ” show responses from the model
 18 with lower labor participation.

19

20 **4.1 Case 1: Effects of an increase in government consumption with**
 21 **complimentary effect on private consumption**

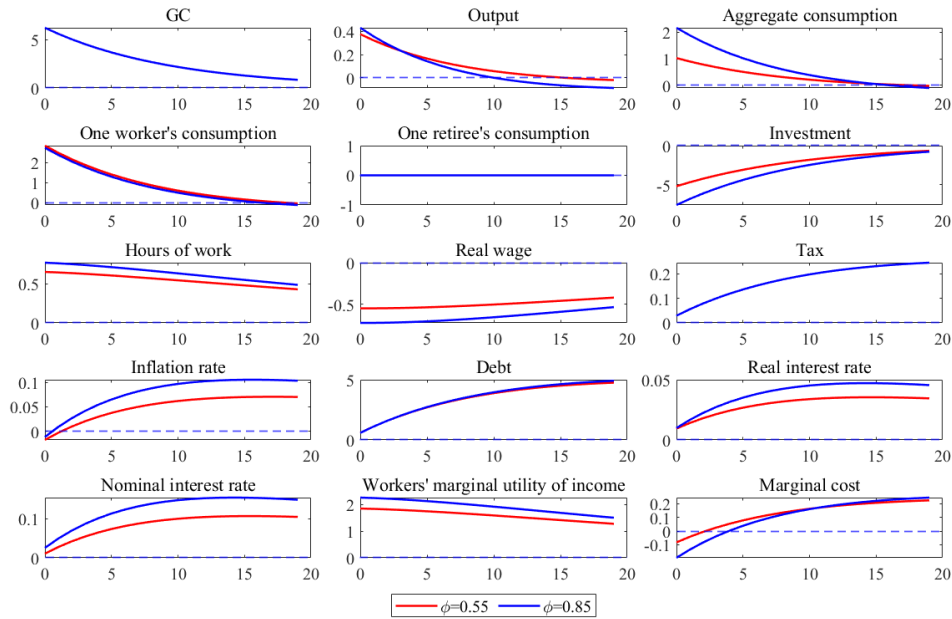
1 Figure 3 shows the impulse responses to a 0.01% GDP increase in
2 government consumption that has the complement effects as shown in Eq. (4).
3 In this case, since the government consumption raises the marginal utility of
4 consumption of workers, it bolsters aggregate consumption to large extent.
5 Therefore, aggregate demand increases more than in the benchmark case,
6 leading to higher demand of labor and capital. However, to compensate the
7 increased consumption, workers supply both factors more than in the
8 benchmark case, causing a greater drop in real factor prices. Similar to the
9 benchmark case, changes in factor prices result in a rise in the marginal costs
10 under our parameter settings, causing an increase in the inflation rate.

11 After this initial shock, government consumption declines gradually. As a
12 result, the marginal utility of private consumption drops down, resulting in a
13 decline in private consumption and the factor supply of workers. As a result,
14 real wages slightly recover, real interest rates rise, and so do nominal interest
15 rates and inflation rates.

16 As seen in the benchmark case, in the aging economy with $\phi=0.55$, the tax
17 burden concentrates on a smaller number of workers, leading to a greater
18 reduction in their consumption. However, since the effect of government
19 consumption on increasing the marginal utility of consumption is stronger when
20 consumption levels are lower, per capita consumption of workers in the aging
21 economy increases more than in the younger economy with $\phi=0.85$, in contrast
22 with the benchmark case. This, in turn, through equations (4) and (5), moderates
23 the increase in labor supply in the aging economy and consequently results in a
24 moderate decrease in wages.

25 Having said that, since there are more workers in the younger economy,
26 aggregate consumption increases more than in the aging economy. Therefore,
27 the impact on output at the initial stage becomes more significant in the younger
28 economy. However, this expansion of consumption through equations (4) and
29 (5), implies a decrease in savings, and the resulting decrease in capital
30 accumulation shrinks production. Thus, the long-term policy effects are smaller
31 in the younger economy.

32



1

2 Figure 3: Impulse responses to a 0.01% increase of GDP in government
3 consumption (Basis point deviation from steady state values)

4

5 Note: Impulse responses reflect basis point deviations from steady-state values.
6 Red lines labeled “ $\phi=0.85$ ” show responses from the model with higher labor
7 participation (i.e. younger economy), while blue lines labeled “ $\phi=0.55$ ” show
8 responses from the model with lower labor participation (i.e. aging economy).

9

10 4.2 Case 2: Effects of an increase in one-time transfer to all generations

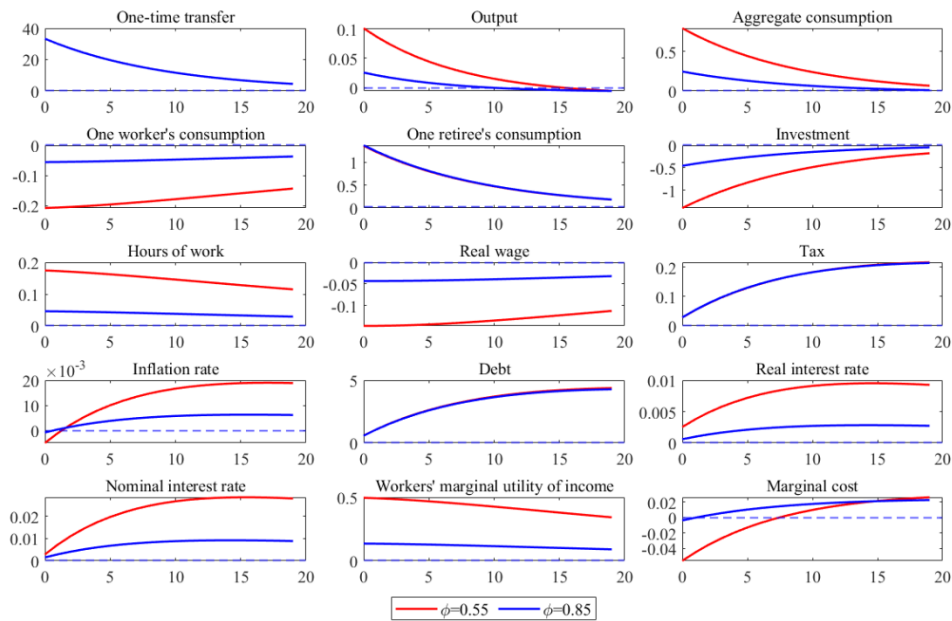
11 Figure 4 shows the impulse responses to a 0.01% increase of GDP in one-
12 time government transfer to all generations. Increased transfers can be
13 interpreted as a combination of increased taxes on workers and increased
14 income to retirees and workers, given that this transfer is financed exclusively
15 by future lump-sum taxes collected from workers. Note that the fact that the
16 complementary effects of government consumption don’t work for one-time
17 transfer.

18 The mechanism of one-time transfer operates as follows: On one hand, the
19 negative wealth effect from tax hikes leads to a decline in consumption of
20 workers. Meanwhile, retirees consume all of the transfers from the government
21 due to their rule-of-thumb behavior. As a result, aggregate consumption

1 increases. The same factor price mechanism explained in the benchmark case,
 2 which increases real interest rates and decreases real wages, is at play here as
 3 well, resulting in a decline in a decrease in inflation rates and nominal interest
 4 rates⁶.

5 In examining the impact of aging on the effectiveness of a one-time transfer
 6 policy under $\phi=0.55$, a crucial observation is that retirees deplete the entire
 7 transfer amount. Consequently, despite the presence of the demand-side aging
 8 effect, aggregate consumption experiences a more pronounced increase in an
 9 aging economy with $\phi=0.55$. The supply-side aging effect leads to a marked
 10 increase in their factor supply, subsequently resulting in a notable decrease in
 11 real wages in the aging economy. Because the effects of real wages on the
 12 marginal cost of intermediate goods surpass those of real interest rates in the
 13 initial period, the marginal costs and inflation rates become negative initially,
 14 then increases along with a rise in the factor prices.

15 Overall, contrasting with the benchmark case, population aging enhances the
 16 demand-side effect of transfer payments, leading to a greater increase in the
 17 inflation rate.
 18



19

⁶ The dynamics of the labor and capital markets are analogous to the case of government consumption in Section 4.1, and therefore, will not be elaborated further.

1 Figure 4: Impulse responses to a 0.01% increase of GDP in one-time transfer.
2 (Basis point deviation from steady state values)

3
4 Note: Impulse responses reflect basis point deviations from steady-state values.
5 Red lines labeled “ $\phi=0.85$ ” show responses from the model with higher labor
6 participation, while blue lines labeled “ $\phi=0.55$ ” show responses from the model
7 with lower labor participation.

9 **4.3 Case 3: Effects of an increase in public investment**

10 Figure 5 depicts the impulse responses to a 0.01% increase in GDP
11 resulting from public investment. On the demand side, public investment works
12 similarly to the benchmark ones. Therefore, the aggregate demand increases.

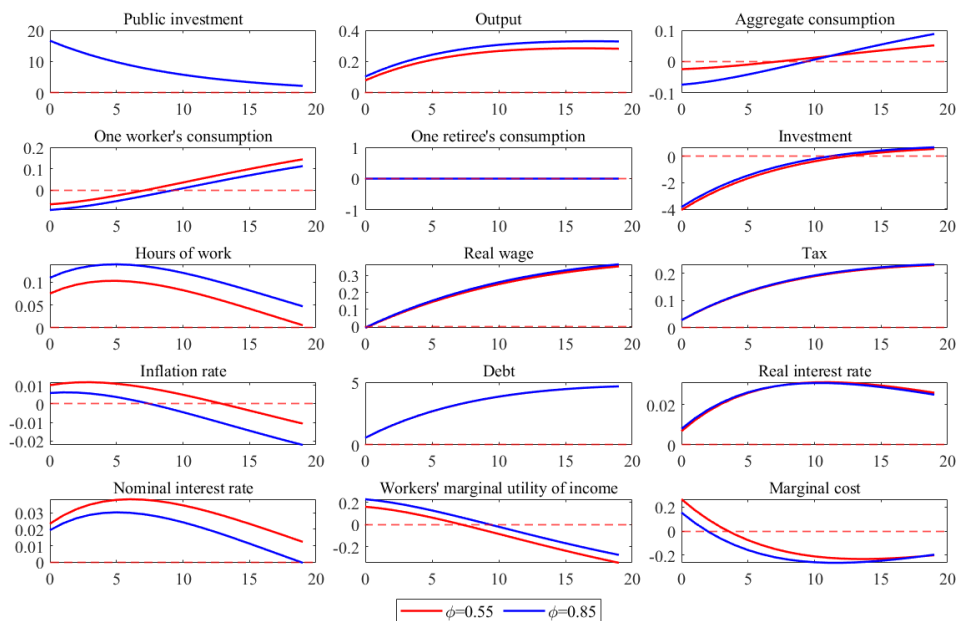
13 Meanwhile, this policy enhances the productivity of intermediate good
14 firms, leading to higher future income rise for workers. Therefore, the increase
15 in factor supply from workers is less than that in the benchmark case.
16 Simultaneously, the increased productivity moderates the factor demand
17 compared to the benchmark. As a result, in the initial period, real wages are
18 almost invariant and real interest rates increase more in contrast to the
19 benchmark case. The mixed effects of this invariant wage and the increased real
20 interest rates initially drive up the marginal costs and inflation rates.

21 Following these initial shocks, public investment starts generating positive
22 externalities in the productivity of intermediate goods, causing their marginal
23 cost to decrease as public capital accumulates. This downward trend leads to a
24 gradual decrease in inflation. The nominal inflation rate reflects these responses
25 through the Taylor rule. In addition, the accumulation of public capital results
26 in an increase in output, which subsequently causes both consumption and
27 investment to respond positively in the medium term.

28 In an aging economy with $\phi=0.55$, the increase in output after public
29 investment becomes lower, but the impact is quantitatively insignificant, as
30 shown on the vertical scale. Qualitatively, the influence of aging manifests as
31 follows:

32 On the demand side, the additional income generated by public investment
33 concentrates on a smaller proportion of workers, and this, in turn, increases
34 consumption per worker. However, the demand-side aging effect works, so a

1 comparatively lower aggregate consumption is observed in an aging economy.
 2 Meanwhile, because of this increased income per worker, the supply-side
 3 aging effects is weakened in the aging economy. Consequently, real wage
 4 decreases in lesser extent and real interest rates increases slightly more. These
 5 make the marginal cost and inflation rate raised up in the same manner so far.
 6 Overall, policy effects are weakened in an aging economy akin to the
 7 benchmark. However, effects of a lowered factor supply support factor prices,
 8 so inflation rates and nominal interest rates are higher under aging.
 9



10
 11 Figure 5: Impulse responses to a 0.01% increase of GDP in public investment.
 12 (Basis point deviations from steady state values)

13
 14 Note: Impulse responses reflect basis point deviations from steady-state values.
 15 Red lines labeled “ $\phi=0.85$ ” show responses from the model with higher labor
 16 participation, while blue lines labeled “ $\phi=0.55$ ” show responses from the model
 17 with lower labor participation.

18
 19 **4.4 Case 4: Effects of an increase in R&D expenditure**

20 Figure 6 illustrates the impulse responses to a 0.01% rise in R&D
 21 expenditure as a percentage of GDP. Its effects differ entirely from the public

1 investment case. The large increase in TFP resulting from government R&D
2 expenditure enhances the lifetime income of workers. Consequently, despite the
3 increased tax burden, there is a *decrease* in labor supply in the initial period.

4 After this initial shock, output remains much higher than that of the
5 benchmark case due to the elevated TFP. This output expansion triggers
6 deflation. Specifically, the improved TFP enhances the marginal productivity of
7 capital and labor for intermediate goods firms, leading to a decrease in demands
8 for both factors. Therefore, despite the decreased labor supply, real wage
9 gradually decreases in the medium term as R&D expenses accumulate.
10 Meanwhile, the decrease in capital demand surpasses an increase in public debt,
11 even considering a reduction in saving, resulting in an immediate decline in real
12 interest rates. These two factors depress the marginal cost of intermediate firms,
13 causing a decline in inflation rate. This deflationary impact results in a decline
14 in nominal interest rates through the Taylor rule.

15 Although the demand effects continue, and the cumulative R&D
16 expenditure enhances TFP, these effects will eventually dissipate. In particular,
17 TFP depreciation is relatively rapid, so the peak of the TFP level is at the eighth
18 period. After that, the TFP level declines, causing the marginal cost increase.
19 This is the reason why responses of the output and the marginal costs exhibit a
20 hump-shaped pattern.

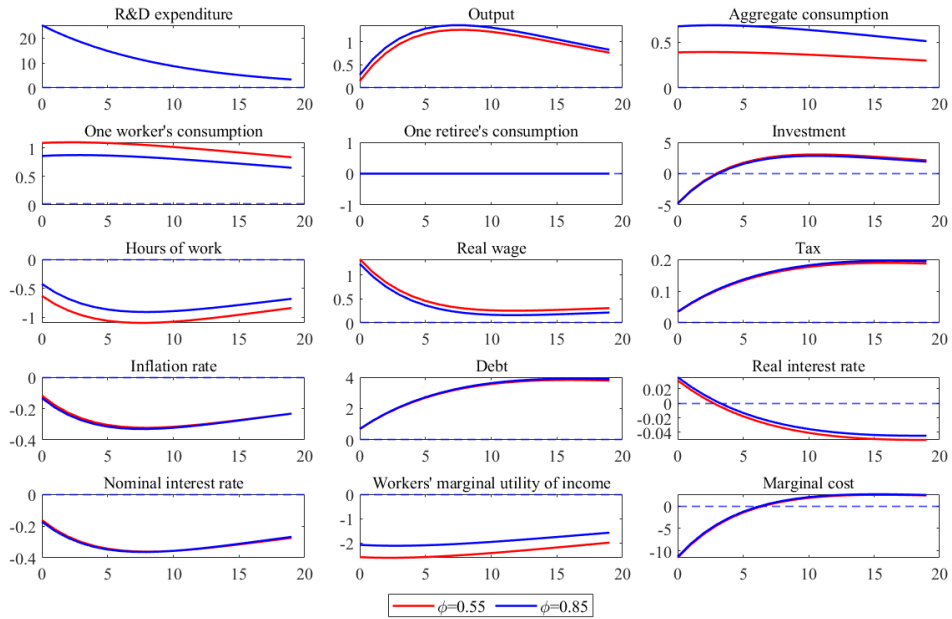
21 Similar to public investment, the quantitative impact of aging on R&D
22 expenditure is insignificant.⁷

23 Since the demand side aging effect is similar to the case of public
24 investment, we observe the lower response of aggregate consumption in an
25 aging economy. On the supply side, workers decrease their labor supply more
26 in an aging economy because of a higher increase in their lifetime income per
27 capita. This leads to an amplification in the rise of real wages. In the capital
28 market, the amplified increase in income elevates worker savings, resulting in a
29 slightly lower real interest rate compared to the case with $\phi = 0.85$. However,
30 changes in factor prices are minimal, resulting in similarly minimal impacts on
31 the marginal cost, inflation rate, and nominal interest rate.

32 Overall, the substantial impact of R&D expenditure on output

⁷ We summarize a difference in aging affects among four types of fiscal spendings in the next section.

1 enhancement diminishes the relative significance of changes brought about by
 2 demographic shifts. The dominant role of R&D investment in driving economic
 3 growth effectively overshadows the effects of population aging.
 4



5
 6 Figure 6: Impulse responses to a 0.01% increase of GDP in R&D expenditure.
 7 (Basis point deviations from steady state values)
 8

9 Note: Impulse responses reflect basis point deviations from steady-state values.
 10 Red lines labeled “ $\phi=0.85$ ” show responses from the model with higher labor
 11 participation, while blue lines labeled “ $\phi=0.55$ ” show responses from the model
 12 with lower labor participation.
 13

1 **4.5 Summary of Policy Comparison**

2 The results of our policy simulation are summarized as follows: Firstly, the
3 the effectiveness of three policies (namely, government consumption, one-time
4 government transfer and public investment) in enhancing GDP-- excluding one-
5 time government transfer-- diminishes with the aging population. This decline
6 is attributed to an increase in the share of policy-irrelevant, stable consumption
7 among retirees in aggregate consumption, which, in turn, weakens demand
8 expansion effect of these three policies. Meanwhile, the transfer exhibits a
9 greater demand expansion effect with aging due to a larger increase in retirees'
10 consumption. On the other hand, because aging concentrates the tax burden and
11 income fluctuations on smaller workers, their savings and labor supply increase,
12 thereby strengthening the policy effect on the supply side. In DSGE models, as
13 policy-induced changes in GDP are generally determined by demand-side
14 policies, they dictate policy effects. Therefore, aging fundamentally weakens
15 the GDP-enhancing effects of policies other than one-time transfers and
16 strengthens the GDP-enhancing effect of one-time transfers. Note that supply-
17 side policy effects significantly influence factor prices and inflation rates.
18 Secondly, regardless of the degree of aging, R&D expenditure consistently
19 emerges as the most effective measure across all time spans. Public investment
20 is identified as the second most effective in the long run, while government
21 consumption takes this position in the short run. The one-time transfer is the
22 least effective in boosting GDP in any time span except for the very short term.
23 If R&D expenditure such as robots which will assist participation of elderly
24 workers into labor force will have bigger impact on the economy since it will
25 increase the value of Φ .

26 27 28 **5. Impact of Aging Population on Fiscal Multipliers and** 29 **Welfares**

30 31 **5-1. Comparison of Fiscal Multipliers by changes in** 32 **demography**

33 To compare the effects of four fiscal spending types and to analyze the

1 impact of supply-side and demand-side aging effects on the multipliers further,
 2 we refer to Mountford and Uhlig (2009) to compute present value output
 3 multipliers under varying demographic structures. These output multipliers are
 4 calculated as follows:

$$5 \quad PV(Y_k|\phi) = \frac{E_0 \sum_{j=0}^k \beta^j \Delta Y_j|\phi}{E_0 \sum_{j=0}^k \beta^j \Delta G_j|\phi}, \quad k \in \{5, 20\}$$

6 where $\Delta Y_j|\phi$ and $\Delta G_j|\phi$ represent the deviations of output and various fiscal
 7 expenditures from their steady states in period j after policy implementation,
 8 under the labor participation rate ϕ .

9 Figure 7 and Table 2 illustrates the short- and long-term fiscal multipliers
 10 under different labor participation rates.

11 A systematic comparison within the same panel reveals the relative
 12 effectiveness of various fiscal policies. Notably, the multiplier for R&D
 13 expenditure outperforms those of other fiscal measures across all demographic
 14 structures and throughout policy implementation timeline, establishing it as the
 15 most effective fiscal policy. Moreover, even in an economy with large amount
 16 of rule-of-thumb retirees, one-time transfer remains the least effective fiscal
 17 expenditure policy. Furthermore, although the short-term multiplier effect of
 18 public investment policies is lower than that of government consumption, its
 19 long-term impact is noteworthy.

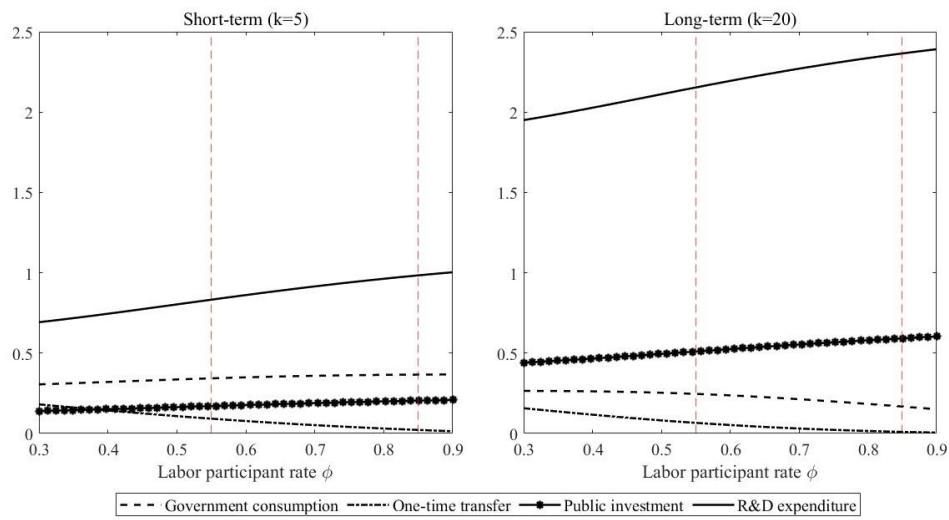
20 Observing the shift of the same policy multipliers across different panels
 21 enables a comparison of policy effectiveness over time. Under any demographic
 22 structure, the multiplier for government consumption generally decreases with
 23 the periods after policy implementation k , suggesting a higher short-term
 24 economic stimulus but weaker long-term effects. The one-time transfer
 25 multiplier remains relatively stable over time. Lastly, the multipliers for public
 26 investment and R&D expenditure, dependent on the accumulation of public
 27 capital and TFP, increase with the duration of policy implementation k .

28 Finally, comparing fiscal multipliers within the same panel allows us to
 29 observe changes in policy effectiveness across different population structures.
 30 In the short term ($k=5$), the demand side aging effect predominates, reducing
 31 the multipliers for government consumption, public investment, and R&D
 32 expenditure with aging, while increasing the multiplier for one-time transfers.
 33 In the long term ($k=20$), the supply side aging effect becomes apparent, while

1 the multiplier for government consumption is weakened.

2 In conclusion, facing population aging, governments should prioritize R&D
 3 expenditures to foster TFP accumulation, in line with the principle of wise
 4 spending. If there are significant barriers to this policy implementation, public
 5 investment emerges as a viable alternative. Lastly, even in the event of a
 6 substantial economic downturn, governments should not consider one-time
 7 transfers as a key component of their policy package.

8



9

10 Figure 7: Present value fiscal multipliers of four fiscal expenditures under
 11 different demographic structures

12

13 Table 2: Output multiplier comparison

	Period after policy implication	Government consumption	One- time transfer	Public Investment	R&D expenditure
Young Population ($\phi = 0.85$)	short-term ($k = 5$)	0.366	0.024	0.203	0.979
	long-term ($k = 20$)	0.171	0.011	0.589	2.359
Old Population ($\phi = 0.55$)	short-term ($k = 5$)	0.342	0.094	0.170	0.830
	long-term ($k = 20$)	0.247	0.068	0.509	2.149

14

5-2. Welfare Comparison

Although the output multiplier is often regarded as an essential tool for assessing the effects of fiscal policies, it is also crucial to measure these policies' efficacy in enhancing social welfare. In the following, we construct a "welfare multiplier" for fiscal expenditures, comparing the impact of different policies on social welfare under various population structures. We construct a national welfare function utilizing the utility functions of workers and retirees as follows:

$$Welfare_t = \phi Welfare_{r,t} + (1 - \phi) Welfare_{w,t},$$

where $Welfare_{w,t}$ and $Welfare_{r,t}$ represent the welfare of workers and retirees, as below.

$$Welfare_{w,t} = \frac{1}{1 - \sigma} \left[\left\{ \omega c_{w,t}^{\frac{\zeta-1}{\zeta}} + (1 - \omega) g_t^{\frac{\zeta-1}{\zeta}} \right\}^{\frac{\zeta}{\zeta-1}} \right]^{1-\sigma} - \frac{h_{w,t}^{1+\mu}}{1 + \mu} + \beta E_t Welfare_{w,t+1},$$

$$Welfare_{r,t} = \frac{1}{1 - \sigma} \left[\left\{ \omega c_{r,t}^{\frac{\zeta-1}{\zeta}} + (1 - \omega) g_t^{\frac{\zeta-1}{\zeta}} \right\}^{\frac{\zeta}{\zeta-1}} \right]^{1-\sigma} + \beta E_t Welfare_{r,t+1}.$$

Similar to the output multiplier, we define the welfare multiplier as follows:

$$PV(Welfare_k|_{\phi}) = \frac{E_0 \sum_{j=0}^k \beta^j \Delta Welfare_j|_{\phi}}{E_0 \sum_{j=0}^k \beta^j \Delta G_j|_{\phi}}, \quad k \in \{5, 20\}$$

Figure 8 and Table 3 show the short- and long-term welfare multipliers under different population structures. Overall, we find that:

Firstly, by comparing the welfare multipliers of different periods and population structures, we find that R&D expenditure has the highest welfare enhancement effect among all policies since R&D shows not only short-run but also long-run impacts on supply side.

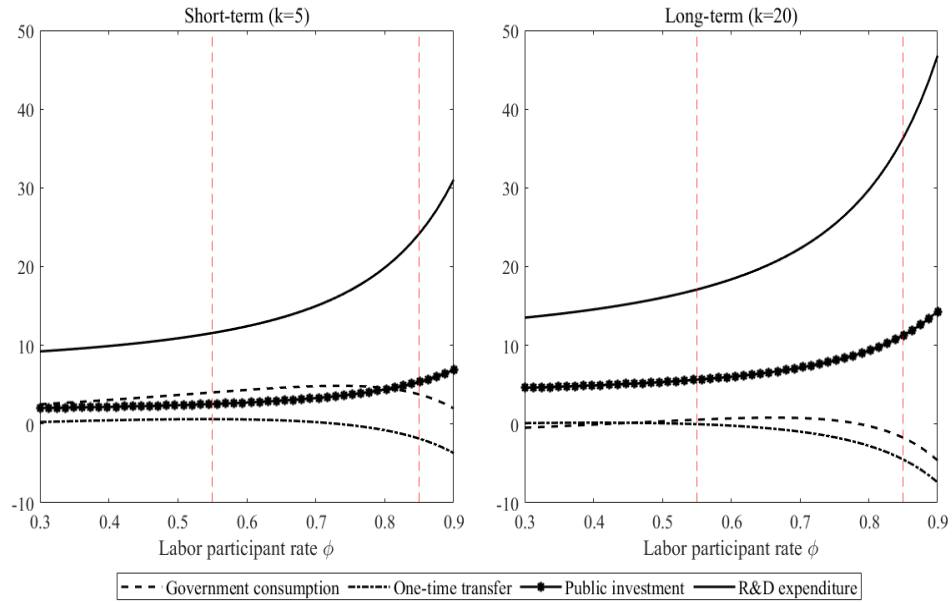
Secondly, the lower the proportion of the elderly population in society, the higher the welfare multiplier of output-promoting policies (public investment, R&D spending). This is primarily because output-promoting policies increase the productivity of workers. As output per labor unit rises, a higher proportion of workers significantly increases the national welfare improvement.

Finally, similar to the output multiplier, the long-term welfare multiplier of output-promoting policies exceeds that of the short-term, whereas it is the opposite for demand-stimulating policies. This is mainly because the production-enhancing effect of output-promoting policies is more pronounced in the long term, fostering consumption. Moreover, in the long term, output-promoting policies reduce workers' labor hours through positive wealth effects. Both factors increase the long-term welfare enhancement effect of output-

1 promoting policies.

2

3



4 Figure 8: Present value welfare multipliers of four fiscal expenditures under
5 different demographic structures

6

7 Table 3: Welfare multiplier comparison

	Period after policy implication	Govern- ment consump- tion	One- time transfer	Public Investme- nt	R&D expendit- ure
Young Population ($\phi = 0.85$)	short-term ($k = 5$)	3.754	-1.548	5.102	24.281
	long-term ($k = 20$)	-1.300	-4.020	10.751	36.478
Old Population ($\phi = 0.55$)	short-term ($k = 5$)	3.990	0.627	2.501	11.490
	long-term ($k = 20$)	0.541	0.008	5.530	16.964

8

9

10 6. Conclusion

11 This study examined the channels through which demographic changes
12 influence the effectiveness of fiscal policies, utilizing four policy tools: (i)
13 government consumption, (ii) one-time government transfers, (iii) public

1 investment, and (iv) R&D expenditures.

2 The findings of our policy simulation are summarized as follows: Firstly,
3 the impact of government consumption, public investment, and R&D
4 expenditure on augmenting GDP diminishes with an aging population. An
5 increase in the share of stable retirees' consumption weakens the
6 macroeconomic response derived from these fiscal expansions. Meanwhile, the
7 effectiveness of the universal one-time government transfer to all generations
8 intensifies with aging. Although aging contributes to increasing savings and
9 labor supply among workers, the demand-side effects overwhelm these effects.

10 Secondly, regardless of the aging level, R&D expenditure consistently
11 emerges as the preeminent measure across all time spans. Public investment
12 takes a secondary position in the long run, while government consumption
13 assumes this role in the short term. The transfer is the least effective in
14 expanding GDP across any temporal scope without a relatively short-term
15 perspective.

16 Thirdly, government consumption multipliers tend to diminish after policy
17 implementation, indicating heightened short-term efficacy but attenuated long-
18 term effects. Multipliers for the transfers persist at a low magnitude, whereas
19 those associated with public investment and R&D expenditure exhibit an
20 upward trajectory contingent upon the accumulation of public capital and TFP.
21 These tendencies become noticeably pronounced with the progression of aging.

22 Much remains for further research. To delve deeper into the channels
23 through which aging impacts the effectiveness of fiscal policy, this study
24 employed a relatively simplified market structure model akin to Yoshino and
25 Miyamoto (2017). However, given the substantial social security pressures
26 induced by aging and their profound implications for public finances,
27 incorporating the financial risks of public debt becomes crucial in future
28 research. Kameda (2014) highlighted that persistent increases in national debt
29 could lead to a rise in long-term interest rates, weakening its effectiveness
30 through the crowding-out effect.

31 For a more comprehensive understanding of this process, future models
32 should incorporate financial frictions like Fernández-Villaverde (2010) and
33 Ashihara and Kameda (2018). These models would specifically analyze how
34 expectations of rising national debt due to aging affect the lending behaviors of

1 the financial sector and how these changes further influence the effectiveness
2 of fiscal policy. This allows for a more detailed analysis of the overarching
3 impacts of aging on the efficacy of fiscal policy.

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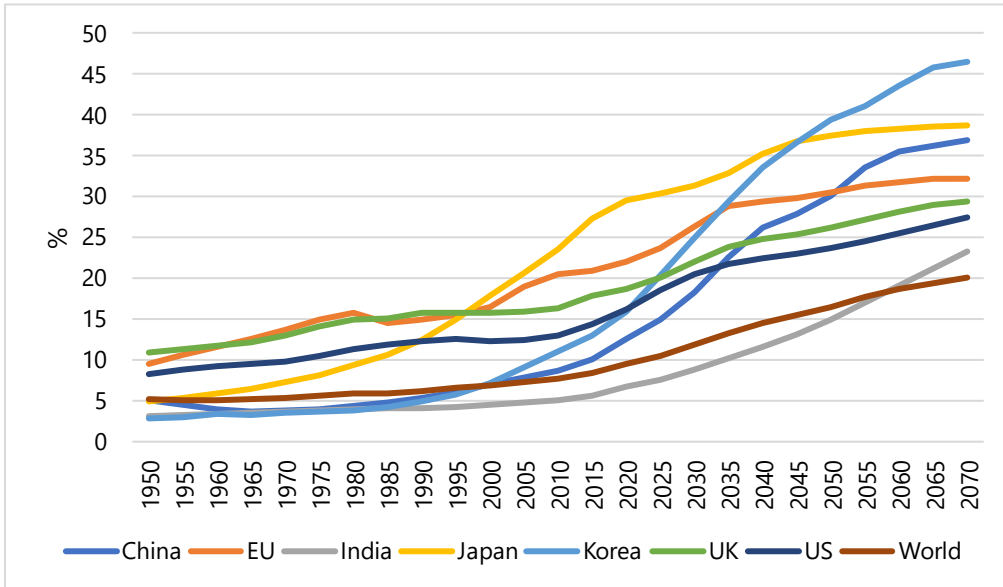
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Figure 1: Share of population aged 65 and older.



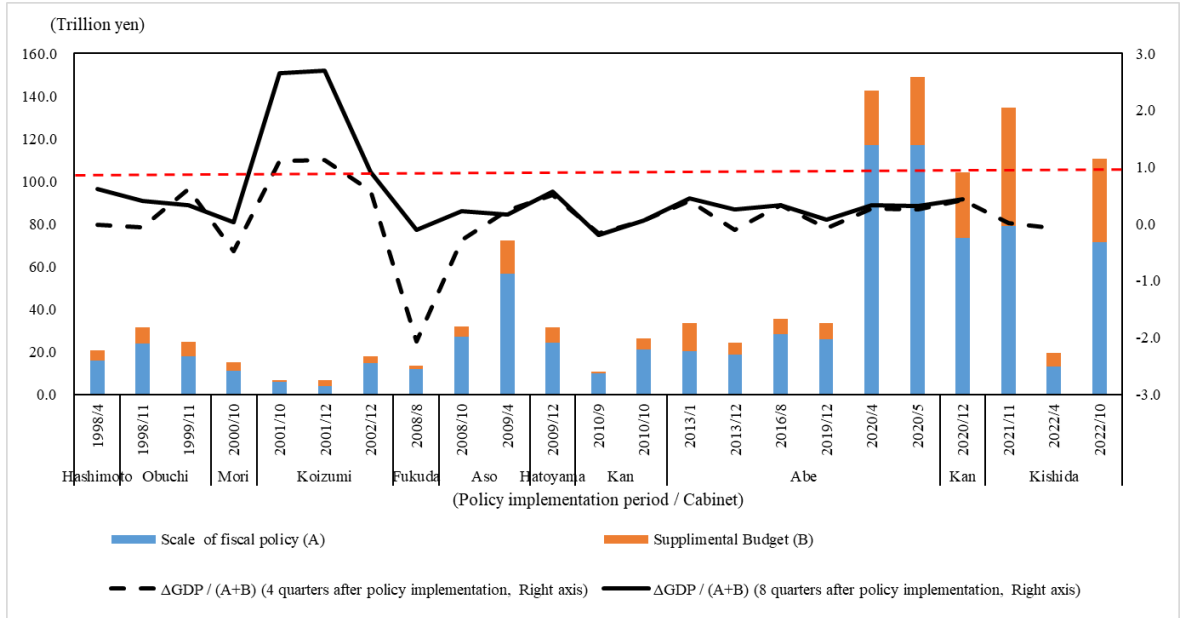
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3 Source: United Nations

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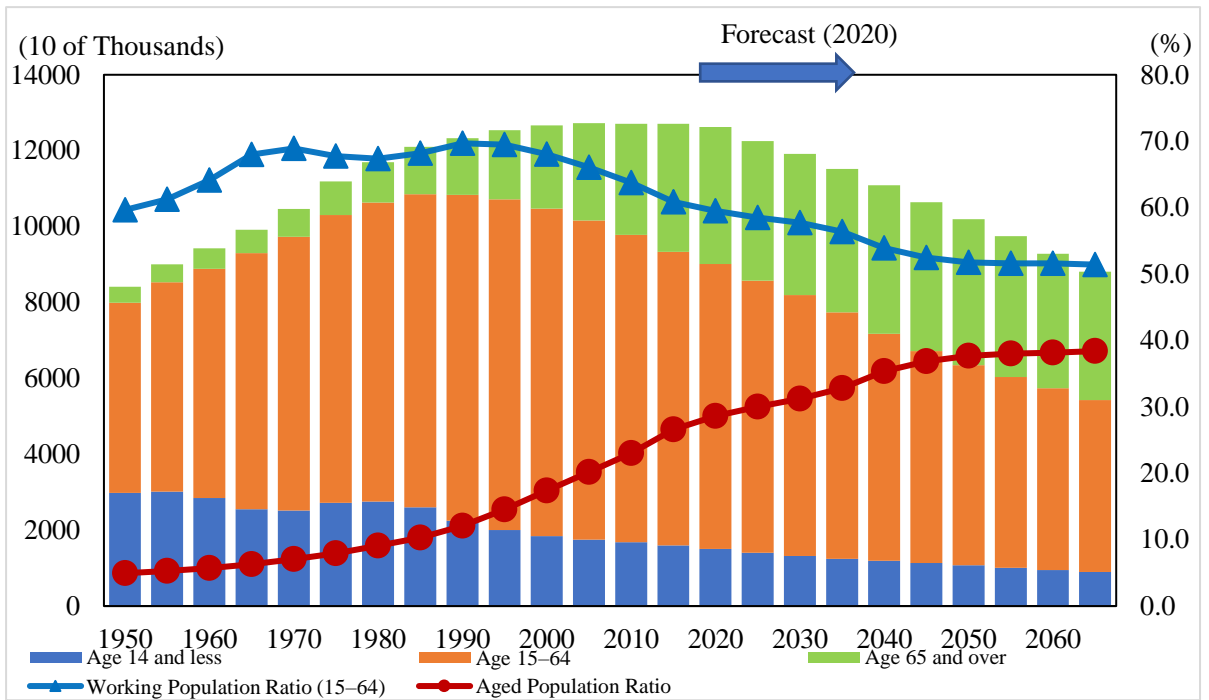
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Source: <https://honkawa2.sakura.ne.jp/5090.html> and Cabinet Office, National

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Accounts of Japan (SNA)

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Figure 2: Population Aging of Japan

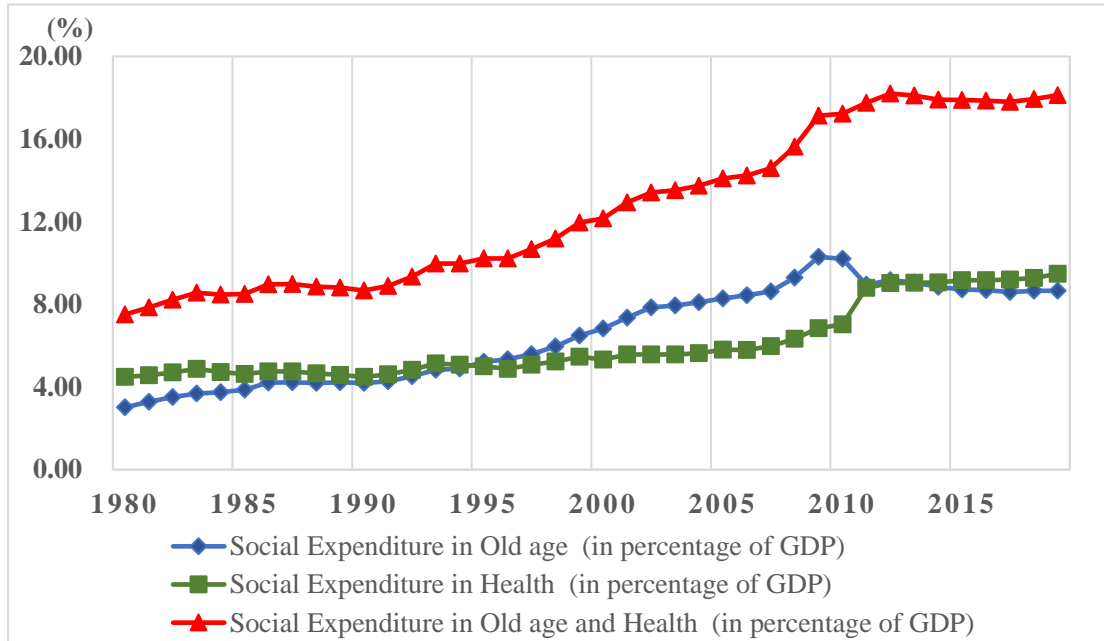
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Source: Ministry of Internal Affairs and Communication

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1 **Figure 3: Social expenditure in health and elderly care (1980–2019)**



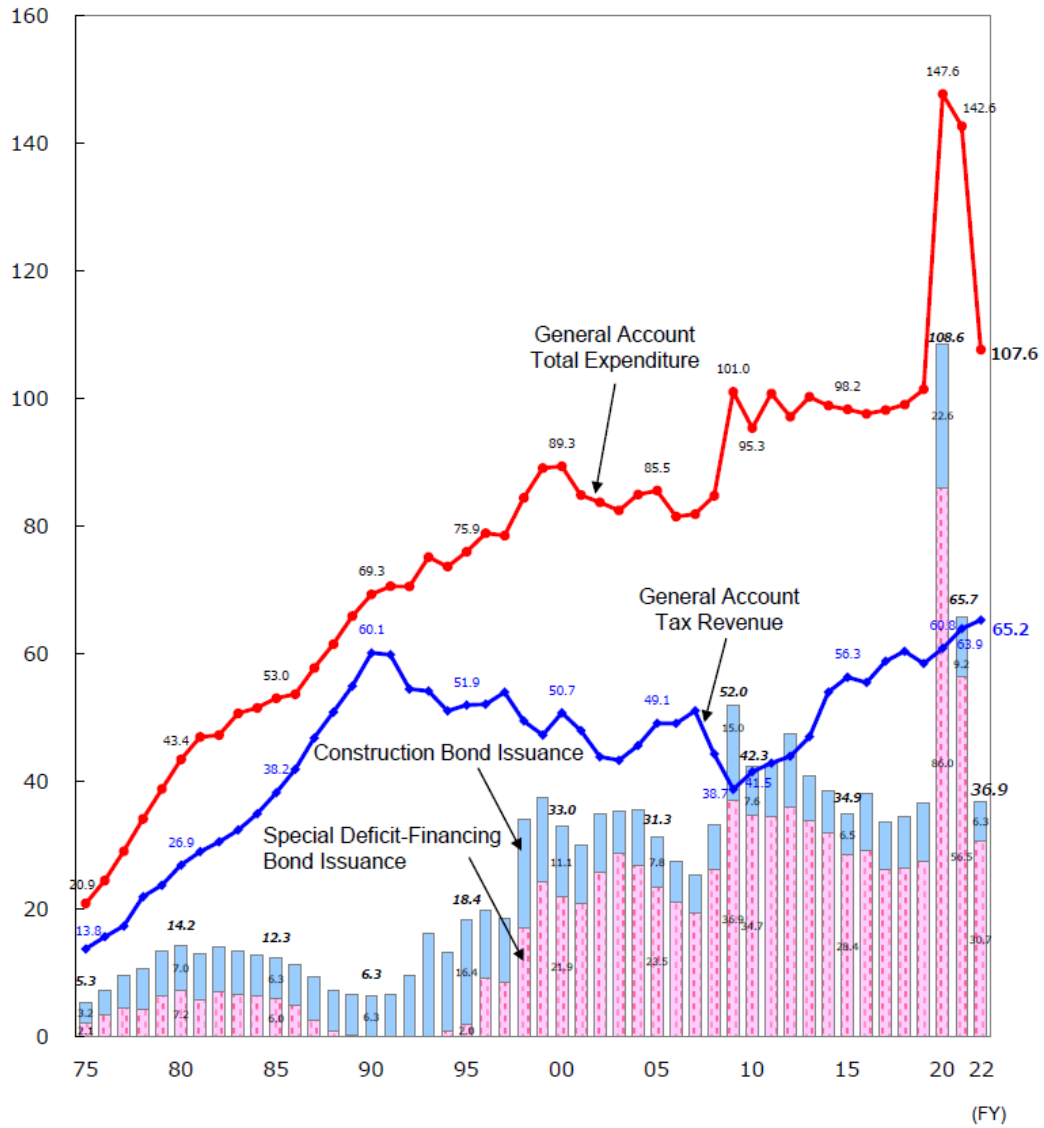
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1 Figure 4: Japan's Government Expenditures and Tax Revenues (Unit:
 2 Trillion Yen)

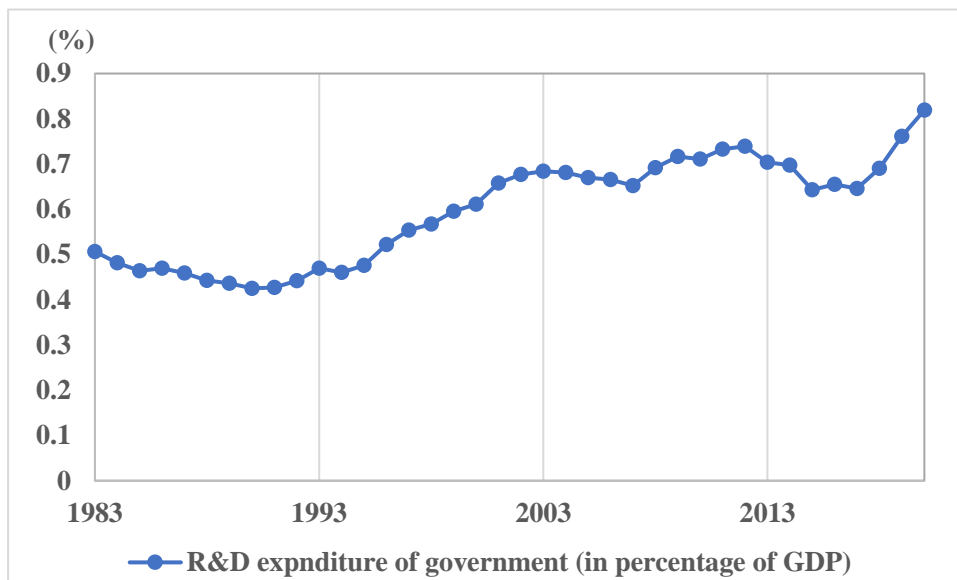


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 4 Source: Ministry of Finance

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1 **Figure 5: R&D expenditure of Japanese government (1980–2019)**

2 Source:



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4 National Institute of Science and Technology Policy (NISTEP)

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